

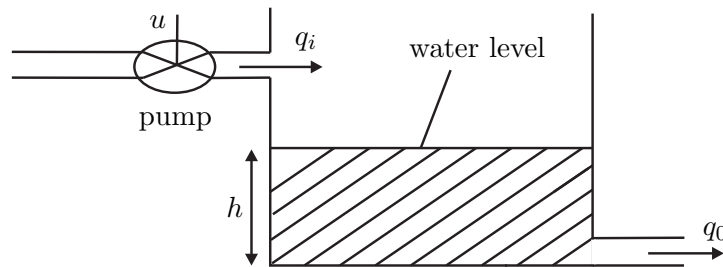
**Exercise Sheet 9: Open-loop Integrators****Problem 18:**

We consider the *one-tank* system in the following figure. The tank with a surface area of  $A$  is connected to a pipe for inflow  $q_i$  [m<sup>3</sup>/sec] and a pipe that leads to outflow  $q_o$  [m<sup>3</sup>/sec]. That is, the height  $h$  of the water-level in the tank is described by the differential equation

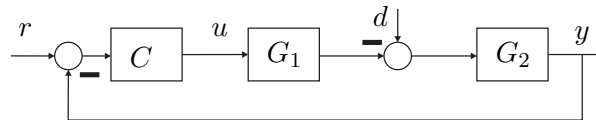
$$\dot{h} = \frac{1}{A}(q_i - q_o).$$

In addition, it is assumed that the water inflow is provided by a pump that is actuated by an input voltage  $u$  and that is characterized by the transfer function (from input  $u$  to inflow  $q_i$ )

$$\frac{Q_i(s)}{U(s)} = G_1(s) = \frac{K_1}{1 + sT_1}$$



The plant can be represented by the following block diagram with the transfer functions  $G_1(s) = \frac{K_1}{1 + sT_1}$  and  $G_2(s) = \frac{1}{sA}$ . The parameters are  $A = .1 \text{ m}^2$ ,  $T_1 = 3 \text{ sec}$  and  $K_1 = 0.03 \text{ m}^3/\text{sec}/\text{V}$ .



- a. Assume that  $C(s) = \frac{P(s)}{L(s)}$  such that  $L(0) \neq 0$ . Show that it holds for disturbance steps that  $\lim_{t \rightarrow \infty} e(t) \neq 0$ .

We now investigate this feedback loop further for  $L(s) = s^i L'(s)$  with  $L'(0) \neq 0$ .

- b. Which value of  $i$  do you need such that disturbance steps are canceled for large times?  
 c. Which value of  $i$  do you need such that disturbance ramps are canceled for large times?  
 d. Assume you choose  $i$  as computed in **c**. Is there overshoot for disturbance steps?

**Problem 19:**

We consider the one-tank system in Problem 18.

- a. Assume the controller  $C(s) = 0.5$  is given. Realize the feedback loop in Simulink and confirm the result in Problem 18 **a**. by simulation.  
 b. Assume that the controller  $C(s) = 0.5 \frac{1 + 10s}{s}$  is given and confirm the result in Problem 18 **b**. by simulation.  
 c. Assume that the controller  $C(s) = \frac{1}{1000} \frac{(1 + 50s)^2}{s^2}$  is given and confirm the results in Problem 18 **c**. and **d**.